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## ABSTRACT

**Iterative closest Point (ICP)** is an algorithm employed to minimize the difference between two point clouds given an initial estimate of the relative pose. It is often used to reconstruct 2D or 3D surfaces from different scans, to localize robots and achieve optimal path planning and to register medical scans. ICP has several steps and each step may be implemented in various ways which give rise to a multitude of ICP variants. In our project, we implement and analyze several variants of ICP, comparing them on the basis of execution speed and quality of the result.

## ITERATIVE CLOSEST POINT ALGORITHM

As indicated above, the algorithm for applying iterative closest point to register a source mesh to a target mesh has several steps. We describe these steps in brief below :

- 1. Selection:** A set of points are selected from the source mesh. In the vanilla implementation, these points are often selected randomly. Selecting more points than less usually leads to a more accurate registration but at the cost of execution speed.
- 2. Matching:** Selected points from the source mesh are transformed via the initial estimated relative pose and matched to the points in the target mesh. The aim here is to pair up points in the two meshes that actually both project to the same point in the real world model.
- 3. Weighting:** The matched points are accordingly weighted. A higher weight is often assigned to a more undesirable pair of matched points. In our implemented variants, we have uniformly weighted all the matched pairs.
- 4. Rejection:** Of the matched points, we reject the outliers - for instance, we may discard the pairs that are separated by a distance greater than some threshold.
- 5. Error metric:** We select an error metric for evaluating the matched pairs. For example, a point to point distance metric, or a point to plane distance metric.
- 6. Optimizing technique:** We must also select an optimization technique for minimizing the error metric for the corresponding pairs from the source and target meshes. For instance, we may opt for linear least squares or non-linear least squares

We will analyze three implementations of ICP that result from a different methodology being used in the steps 1, 2 and 6 of the algorithm as outlined in the above section.

## IMPLEMENTED VARIANT : BASELINE

The baseline ICP we use has the following features:

- A fixed number of points are randomly selected from the source mesh.
- An attempt is made to match all of the selected points to points in the target mesh by means of a kd tree and Nearest Neighbor approach
- Matched pairs are rejected if the distance between them is greater than a fixed threshold
- The error metric to be minimized is selected to be the sum of the point to plane distance between all the matched pairs
- A Non-linear least squares optimization technique, specifically Levenberg-Marquardt [4] and [5], is used to minimize the error. We run the optimization for 10 iterations for the RGBD-Dataset.

## IMPLEMENTED VARIANT : LINEARIZED ICP

In this variant, we replace the baseline's optimization algorithm (Step 6 from Iterative Closest Point Algorithm) - Levenberg-Marquardt (LM) with Singular Value Decomposition (SVD).

LM is an iterative technique for optimization of a non-linear least squares problem - a generalization of linear least squares. SVD, on the other hand is a stable technique for solving a system of linear equations in one shot.

So, while LM can be used to optimize more generalized error functions that may be changing with each iteration (as in ICP), SVD is much quicker, not just because it may converge in one iteration (we also used it for the same number of iterations as the baseline), but also because it takes less compute time than LM which has to calculate Jacobians at each iteration.

## DATASET : WE PERFORM OUR ANALYSIS ON TWO DATASETS

### 1. Bunny Meshes

We use the bunny meshes from the exercise [6] to demonstrate the effects of the different variants of Iterative Closest Point. Initially, the source (green) and the target (red) meshes are aligned as below:

### 2. RGBD Freiburg - xyz

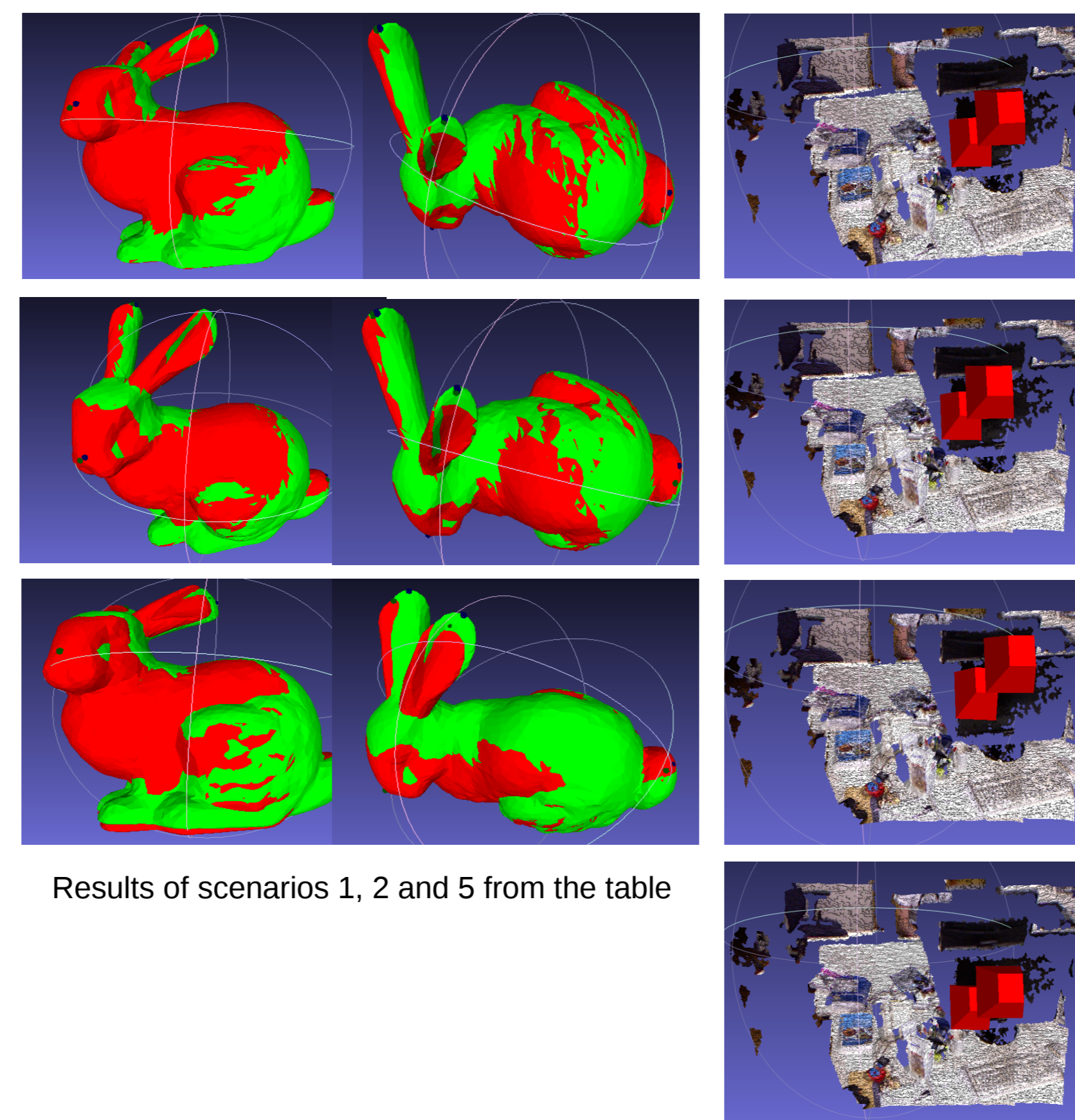
This data was taken from a public dataset from the Computer Vision Group, TUM. [7]. For this sequence, the Kinect was pointed at a typical desk in an office environment. This sequence contains only translatory motions along the principal axes of the Kinect, while the orientation was kept (mostly) fixed. Initially, the source and the target meshes are aligned as below:

## EXPERIMENTAL RESULTS

Combinations of Steps 1,2,6	Completion Time	L2 error from known correspondences	Output Quality
1. Random Sampling, NN <sup>1</sup> and LM <sup>2</sup>	Dataset 1: 0.12035s Dataset 2: 196.876s	Dataset 1: 0.0157368 Dataset 2: N/A	Registration Quality is good in both Datasets <sup>6</sup>
2. Multi-Resolution, NN <sup>1</sup> and LM <sup>2</sup>	Dataset 1: 0.09897s Dataset 2: 105.661s	Dataset 1: 0.0162046 Dataset 2: N/A	Registration Quality is good in both Datasets <sup>6</sup>
3. Random Sampling, Projective (Neighborhood of 5 px) and LM <sup>2</sup>	Dataset 1: N/A Dataset 2: 133.704s	Dataset 1: N/A Dataset 2: N/A	Registration Quality is good in both Datasets <sup>6</sup>
4. Random Sampling, NN <sup>1</sup> and SVD <sup>3</sup> (1 iteration)	Dataset 1: 0.04029s Dataset 2: 27.1635s	Dataset 1: 0.13298 Dataset 2: N/A	Fails <sup>4</sup> in Dataset 1, Good <sup>5</sup> for Dataset 2
5. Random Sampling, NN <sup>1</sup> and SVD <sup>3</sup>	Dataset 1: 0.06189s Dataset 2: 85.9964s	Dataset 1: 0.0370271 Dataset 2: N/A	Registration Quality is good in both Datasets <sup>6</sup>
6. Multi-Resolution, Projective (Neighborhood of 5 px) and SVD <sup>3</sup>	Dataset 1: N/A Dataset 2: 29.106s	Dataset 1: N/A Dataset 2: N/A	Registration Quality is good in both Datasets <sup>6</sup>

<sup>1</sup> Nearest Neighbor Search  
<sup>2</sup> Levenberg-Marquardt  
<sup>3</sup> Singular Value Decomposition

<sup>4</sup> and <sup>5</sup> While SVD (1 iteration) works well with the Freiburg dataset, it fails to completely align the bunny meshes (see Fig 3). This could be because while in the Freiburg dataset, the input meshes were very close (or rather the initial relative pose was nearly accurate), but the bunny meshes were quite some distance apart. Repeated iterations of SVD seemed to align both meshes quite well, however.  
<sup>6</sup> All the outputs are more or less comparable



Results of scenarios 1, 2 and 5 from the table

Results of scenarios 1, 3, 5 and 6 from the table

## IMPLEMENTED VARIANT : MULTI-RESOLUTION ICP

We introduce a different methodology for step 1 in this scheme. Instead of selecting a fixed number of source points for matching, we change the number of points to be matched as we iterate, effectively moving from matching a coarse resolution of the source mesh to matching a fine resolution of the source mesh (more number of points) as we iterate and refine our solution. Our implementation follows the multiresolution scheme outlined in [1].

We sample about one eighth of the total source pixels - this is our richest resolution. We resample these points twice to give us our 2nd and third resolutions (see Fig 1). We match the points first in the coarsest resolution and then, as we move through our fixed number of iterations, we increase the resolution.



Fig 1: Resolution 1 to 3 range from the finest to the coarsest resolutions. The deep blue squares are indicative of the source points selected for each of the resolutions. We keep sampling one eighth of the points from the sample space to get a coarser resolution.

Lessening the number of points in the first few steps results in less accurate registration, but as the resolution is increased in the subsequent iterations, the result improves as well. Additionally, we still have the benefit of a faster convergence speed over the vanilla implementation.

## IMPLEMENTED VARIANT : PROJECTIVE ICP

In our baseline implementation of ICP, we use Nearest-Neighbors for calculating matches (Step 2 from Iterative Closest Point Algorithm). Here, we use a much faster method based on the paper by Blais and Levine [2]

Instead of searching for a neighbor in the whole space of sampled points from the target, we leverage the structure of our 2D image projection of the 3D scene to automatically calculate the closest point in the target sample space (or a tighter search neighborhood for our source point) (see Fig 2).

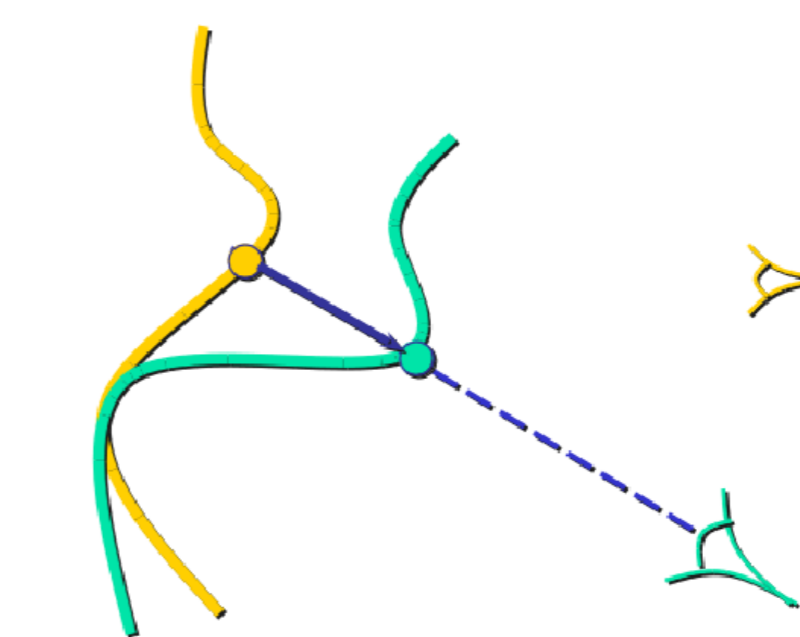


Fig 2: Project the sampled point from the source onto the target mesh, from the point of view of the target mesh's camera (image taken from [3])

We describe the algorithm for matching in projective ICP below:

- Transform a sampled source point by its estimated relative transformation. The initial value for this is often taken to be identity
- Project this transformed point on to the target image plane, thus obtaining the row (r) and column (c) of the pixel it maps to.
- Project the pixel at (r,c) in the target image back to the 3D camera space.
- Calculate the point to plane distance between the transformed point and the matched target point
- Discard the match if the distance is beyond the fixed threshold. If not, add to the error metric.

This scheme may result in a faster convergence rate as we decrease the neighborhood search area. The search window size dictates the accuracy of the solution and the speed of the algorithm. Increasing the size of the search window results in a higher accuracy but the speed of execution decreases.

## REFERENCES

- [1] T. Jost and H. Hugli, "A multi-resolution ICP with heuristic closest point search for fast and robust 3D registration of range images", Fourth International Conference on 3-D Digital Imaging and Modeling, 2003. 3DIM 2003. Proceedings.
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## CONCLUSION

As noted, using a Multi-resolution approach, Projective Correspondences and SVD lead to a significant gain in speed as compared to baseline approach.

In fact, a combination of the three approaches is nearly seven times faster than the baseline. However, this may come at a slight cost in quality as observed from the L2 errors calculated, particularly in the case of SVD vs LM. This was expected as LM can solve much more complex problems than a linear approach like SVD.

Nevertheless, we believe that the cost in quality is sufficiently low, making it a very good case for SVD